## Appendix A

## Fuzzy Set Theory \& Fuzzy Logic Concepts

## A. 1 Fuzzy Set

Members of a Crisp set take the value either 0 or 1 . But members of a fuzzy set can take any value between 0 and 1 , means it can take partial memberships. Thus a fuzzy set $A$ in the universe of discourse $U$ may be represented as a set of ordered pairs of element "u" and its membership grade " $\mu_{\overline{\mathrm{A}}}(u)$ ", and it can be written as

$$
\overline{\mathrm{A}}=\left\{\left(u, \mu_{\overline{\mathrm{A}}}(u)\right) / u \in U\right\} .
$$

When $U$ is continuous, a fuzzy set $A$ can be written as

$$
\bar{A}=\int_{U} \mu_{\bar{A}}(u) / u
$$

When $U$ is discrete, a fuzzy set $A$ is represented as

$$
\bar{A}=\sum_{i=1}^{n} \mu_{\bar{A}}\left(u_{i}\right) / u_{i}
$$

## A. 2 Membership Function

Every Fuzzy Set has linguistic classes. Each linguistic class has its own definition about how \& when each element in the universe of discourse can become the member of that linguistic class. This definition about belonging is called "membership function" of that class. Figure 11 gives different membership functions and its graphical representation.

## A. 3 Fuzzy Operations: Union \& Intersection

If ${ }^{\bar{P}}$ and ${ }^{\bar{Q}}$ be two fuzzy sets in U with membership functions $\mu_{\bar{P}}$ and $\mu_{\bar{Q}}$ respectively then union, intersection of them can be written as ${ }^{\mu_{\bar{\Omega} \bar{Q}}}$ for the union $\bar{P} \cup \bar{Q}$ and ${ }^{\mu_{\mathrm{A} \cap \mathrm{B}}}$ for ${ }^{\bar{P} \cap \bar{Q}}$ and can be written as

$$
\begin{aligned}
& \mu_{\overline{\mathrm{P}, \bar{Q}}}=\max \left\{\mu_{\bar{p}}(u), \mu_{\bar{Q}}(u)\right\} \text { for all } \mathbf{u} \in \mathrm{U} \\
& \mu_{\overline{\mathrm{P}} \cap \bar{Q}}=\min \left\{\mu_{\bar{P}}(u), \mu_{\bar{Q}}(u)\right\} \text { for all } \mathbf{u} \in \mathrm{U}
\end{aligned}
$$

## A. 4 Fuzzy Rules

Fuzzy rule contains antecedents (the inputs) and consequents (the output). Antecedents may contain a single fuzzy set or may contain union or intersection of many fuzzy sets and Consequents normally refer to single fuzzy set for every rule. An example of fuzzy rule is

$$
\text { If } \bar{P} \text { is ' } x^{\prime} \text { and } \bar{Q} \text { is ' } y^{\prime} \text { then } \bar{R} \text { is ' } z^{\prime}
$$

Where $\mathrm{x}, \mathrm{y}$ and z are the linguistic classes represented either by words or by numbers. A typical example of fuzzy rule is

If Ecolsus is 'Good' and Econsus is 'Good' and Socsus is 'Satisfactory' Then Osus is 'Good'

In most of the cases we may have to deal with group of input fuzzy rules, which leads to many output combinations, but as a total we are interested in the single output. In such cases Sup-Star compositions like Min [max ()] or Max [min ()], helps to integrate all of them. In the current research Max $[\min ()]$ composition is used, which means that the from the Antecedents groups, minimum value will be considered for every rule and from these outputs maximum values will be considered for final aggregation. In short we can say that UNION [INTERSECTION ()]. The output value of every rule will also have attached "linguistic class" and hence the reasoning stands valid irrespective of the value.

## A.5. Fuzzy Inference

Fuzzy inference refers to the internal mechanism for producing output values for a given value through fuzzy rules. In short the inference process involves 3 steps: fuzzification, rule evaluation and defuzzification. Fuzzification process converts the input real world values or standardized values into grades of memberships and corresponding linguistic classes. These fuzzified grades/classes are evaluated through fuzzy rules for output grades/classes. Finally these output grades are again converted back to real world crisp output values through centroid calculation in defuzzification
process. There are 2 known inference methods: Mamdani's approach and Sugeno approach. Mamdani approach considers complete fuzzy set for centroid calculation in defuzzification, but Sugeno approach take the Singletons as the highest membership value and corresponding x-point of output aggregated fuzzy set and finds the weighted average of these singletons as defuzzified output value.

## A.4.1 Rule Implication \& Aggregation Process

The implication process evaluates individual rule over fuzzified grades and generates an output grade and output class. Now the Aggregation does 2 things. First it truncates the Consequent Fuzzy Set according to the grade obtained and secondly it does the Union of all these fuzzy sets.


Figure A.1. Fuzzy Mamdani Inference over Indicator ISS and FFS for aggregation
Rule $5=$ If (ISS) is (medium) and FFS is (medium) then SOCsus is satisfactory
Rule $6=$ If (ISS) is (medium) and FFS is (high) then SOCsus is Good

## A.4.2 Defuzzification

Defuzzification process calculates the output crisp value from the aggregated resultant fuzzy set derived after rule evaluation. There are different ways of calculating output value, but widely used methods are: Center of gravity method and Height method. In the centroid method all the elements within the aggregated fuzzy sets are considered with its respective memberships and it Height method only Mean of Maximum membership value and its corresponding x-element are considered.

Example:

Let us consider Indicator Socsus, with normalized values 0.43 for the primary indicator ISS and 0.93 for FFS. Fuzzified values (Yj) for ISS and FFS are 0.75 . There is only one possible combination Rule 6 [If (ISS) is (medium) and FFS is (high) then SOCsus is Good] is activated. The result of Rule 6 is (Good) with the grade $\mu$ TSOCsus $=(0.1060,0.75)$. Now the aggregation process truncates the good fuzzy set with the grade $(0.1062,0.75)$. Then finally output crisp value is calculated.

$$
\begin{aligned}
\operatorname{Def}(\text { TSOCsus })= & \frac{\sum_{j} Y j * \mu \operatorname{TSOCsus}(Y j)}{\sum_{j} \mu T S O C s u s(Y j)} \\
& =\frac{(0.75 * 0.1062)+(0.75 * 0.75)}{0.1062+0.75} \\
& =0.75
\end{aligned}
$$

Center of gravity


FigureA. 2 : Defuzzification Process

## Appendix B

## Fuzzy Rules used at different levels

The process of adquiring fuzzy rule is an important process in fuzzy logic approach. Number of rules depends upon the number of linguistic classes present for each input parameter. If the number of linguistic classes are 5 and number of input variables are 2 then $5 * 5=25$ rules are needed. In general form, number of rules needed can be written as $\mathrm{L}^{\mathrm{n}}$, where L is the number of linguistic classes and n refers to number of input variables.

For secondary variables; UCF $\qquad$ FFS, are associated with 3 linguistic classes. Primary variables; ECOLsus, ECONsus, SOCsus and Osus are 5 linguistic classes.

For aggregation of ECOLsus, $3^{4}=81$ rules are needed.
For aggregation of ECONsus, $3^{3}=27$ rules are needed.
For aggregation of SOCsus, $3^{2}=9$ rules are needed.
For aggregation of Osus, $5^{3}=125$ rules are needed. For each aggregation, the applied rules are presented in Figure B. 1 and Table B.1.


Figure B.1. Number of Rules required at different levels of aggregation

Table B.1. Rule application for overall sustainability assessment (125 Rules)

| No. | IF (ECOLsus)= | AND (ECONsus)= | $\begin{aligned} & \text { AND } \\ & \text { (SOCsus)= } \end{aligned}$ | THEN (Osus)= |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Vbad | Vbad | Vbad | Vbad |
| 2 | Vbad | Vbad | Bad | Vbad |
| 3 | Vbad | Vbad | Satisfactory | Bad |
| 4 | Vbad | Vbad | Good | Bad |
| 5 | Vbad | Vbad | Vgood | Bad |
| 6 | Vbad | Bad | Vbad | Vbad |
| 7 | Vbad | Bad | Bad | Bad |
| 8 | Vbad | Bad | Satisfactory | Bad |
| 9 | Vbad | Bad | Good | Bad |
| 10 | Vbad | Bad $\square$ | Vgood | Bad |
| 11 | Vbad | Satisfactory | Vbad | Bad |
| 12 | Vbad | Satisfactory | Bad | Bad |
| 13 | Vbad | Satisfactory | Satisfactory | Bad |
| 14 | Vbad | Satisfactory | Good | Bad |
| 15 | Vbad | Satisfactory | Vgood | Bad |
| 16 | Vbad | Good | Vbad | Bad |
| 17 | Vbad | Good | Bad | Bad |
| 18 | Vbad | Good | Satisfactory | Bad |
| 19 | Vbad | Good | Good | Bad 5 |
| 20 | Vbad | Good | Vgood | Bad |
| 21 | Vbad | Vgood | Vbad | Bad |
| 22 | Vbad | Vgood | Bad | Bad |
| 23 | Vbad | Vgood | Satisfactory | Bad |
| 24 | Vbad | Vgood | Good | Bad |
| 25 | Vbad | Vgood | Vgood | Bad |
| 26 | Bad | Vbad | Vbad | Bad |
| 27 | Bad | Vbad | Bad | Bad |
| 28 | Bad | Vbad | Satisfactory | Bad |
| 29 | Bad | Vbad | Good | Bad |
| 30 | Bad | Vbad | Vgood | Bad |
| 31 | Bad | Bad | Vbad | Bad |
| 32 | Bad | Bad | Bad | Bad |
| 33 | Bad | Bad | Satisfactory | Bad |
| 34 | Bad | Bad | Good | Bad |
| 35 | Bad | Bad | Vgood | Bad |
| 36 | Bad | Satisfactory | Vbad | Bad |
| 37 | Bad | Satisfactory | Bad | Bad |
| 38 | Bad | Satisfactory | Satisfactory | Satisfactory |
| 39 | Bad | Satisfactory | Good | Satisfactory |
| 40 | Bad | Satisfactory | Vgood | Satisfactory |
| 41 | Bad | Good | Vbad | Bad |
| 42 | Bad | Good | Bad | Bad |
| 43 | Bad | Good | Satisfactory | Satisfactory |
| 44 | Bad | Good | Good | Satisfactory |
| 45 | Bad | Good | Vgood | Satisfactory |
| 46 | Bad | Vgood | Vbad | Bad |


| Table B. 1 (continued) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 47 | Bad | Vgood | Bad | Bad |
| 48 | Bad | Vgood | Satisfactory | Satisfactory |
| 49 | Bad | Vgood | Good | Satisfactory |
| 50 | Bad | Vgood | Vgood | Satisfactory |
| 51 | Satisfactory | Vbad | Vbad | Bad |
| 52 | Satisfactory | Vbad | Bad | Bad |
| 53 | Satisfactory | Vbad | Satisfactory | Bad |
| 54 | Satisfactory | Vbad | Good | Bad |
| 55 | Satisfactory | Vbad | Vgood | Bad |
| 56 | Satisfactory | Bad | Vbad | Bad |
| 57 | Satisfactory | Bad | Bad | Bad |
| 58 | Satisfactory | Bad | Satisfactory | Satisfactory |
| 59 | Satisfactory | Bad | Good | Satisfactory |
| 60 | Satisfactory | Bad | Vgood | Satisfactory |
| 61 | Satisfactory | Satisfactory | Vbad | Bad |
| 62 | Satisfactory | Satisfactory | Bad | Satisfactory |
| 63 | Satisfactory | Satisfactory | Satisfactory | Satisfactory |
| 64 | Satisfactory | Satisfactory | Good | Satisfactory |
| 65 | Satisfactory | Satisfactory | Vgood | Good |
| 66 | Satisfactory | Good | Vbad | Bad |
| 67 | Satisfactory | Good | Bad | Satisfactory |
| 68 | Satisfactory | Good | Satisfactory | Satisfactory |
| 69 | Satisfactory | Good | Good | Good |
| 70 | Satisfactory | Good | Vgood | Good |
| 71 | Satisfactory | Vgood | Vbad | Bad |
| 72 | Satisfactory | Vgood | Bad | Satisfactory |
| 73 | Satisfactory | Vgood | Satisfactory | Good |
| 74 | Satisfactory | Vgood | Good | Good |
| 75 | Satisfactory | Vgood | Vgood | Good |
| 76 | Good | Vbad | Vbad | Vbad |
| 77 | Good | Vbad | Bad | Bad |
| 78 | Good | Vbad | Satisfactory | Bad |
| 79 | Good | Vbad | Good | Bad |
| 80 | Good | Vbad | Vgood | Bad |
| 81 | Good | Bad | Vbad | Bad |
| 82 | Good | Bad | Bad | Bad |
| 83 | Good | Bad | Satisfactory | Satisfactory |
| 84 | Good | Bad | Good | Satisfactory |
| 85 | Good | Bad | Vgood | Satisfactory |
| 86 | Good | Satisfactory | Vbad | Bad |
| 87 | Good | Satisfactory | Bad | Satisfactory |
| 88 | Good | Satisfactory | Satisfactory | Satisfactory |
| 89 | Good | Satisfactory | Good | Good |
| 90 | Good | Satisfactory | Vgood | Good |
| 91 | Good | Good | Vbad | Bad |
| 92 | Good | Good | Bad | Satisfactory |
| 93 | Good | Good | Satisfactory | Good |
| 94 | Good | Good | Good | Good |
| 95 | Good | Good | Vgood | Good |
| 96 | Good | Vgood | Vbad | Bad |
| 97 | Good | Vgood | Bad | Satisfactory |
| 98 | Good | Vgood | Satisfactory | Good |


| Table B.1 (continued) |  |  |  | Good |
| :--- | :--- | :--- | :--- | :--- |
| 99 | Good | Vgood | Vgood | Good |
| 100 | Good | Vbad | Vbad | Vgood |
| 101 | Vgood | Vbad | Bad | Bad |
| 102 | Vgood | Vbad | Satisfactory | Bad |
| 103 | Vgood | Vbad | Good | Bad |
| 104 | Vgood | Vbad | Vgood | Bad |
| 105 | Vgood | Bad | Vbad | Bad |
| 106 | Vgood | Bad | Sad | Batisfactory |
| 107 | Vgood | Bad | Good | Satisfactory |
| 108 | Vgood | Bad | Vgood | Satisfactory |
| 109 | Vgood | Satisfactory | Vbad | Satisfactory |
| 110 | Vgood | Satisfactory | Bad | Bad |
| 111 | Vgood | Satisfactory | Satisfactory | Satisfactory |
| 112 | Vgood | Satisfactory | Good | Satisfactory |
| 113 | Vgood | Satisfactory | Vgood | Good |
| 114 | Vgood | Good | Vbad | Good |
| 115 | Vgood | Good | Bad | Bad |
| 116 | Vgood | Good | Satisfactory | Satisfactory |
| 117 | Vgood | Good | Good | Good |
| 118 | Vgood | Good | Vgood | Good |
| 119 | Vgood | Vgood | Vbad | Vgood |
| 120 | Vgood | Vgood | Bad | Bad |
| 121 | Vgood | Vgood | Satisfactory | Satisfactory |
| 122 | Vgood | Vgood | Good | Good |
| 123 | Vgood | Vgood | Vgood | Vgood |
| 124 | Vgood |  |  |  |
| 125 | Vgood |  |  |  |
|  |  |  |  |  |

Table B.2. Rule application for Environmental sustainability assessment (81 Rules)

| No. | IF (UCF)= | AND (UOF)= | $\begin{aligned} & \begin{array}{l} \text { AND } \\ (\mathrm{CLC})= \end{array} \end{aligned}$ | $\begin{aligned} & \hline \text { AND } \\ & \text { (CCuse) }= \end{aligned}$ | $\begin{aligned} & \hline \text { THEN } \\ & \text { (ECOLsus)= } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Low | Low | Low | Low | Vbad |
| 2 | Low | Low | Low | Medium | Vbad |
| 3 | Low | Low | Low | High | Vbad |
| 4 | Low | Low | Medium | Low | Vbad |
| 5 | Low | Low | Medium | Medium | Bad |
| 6 | Low | Low | Medium | High | Bad |
| 7 | Low | Low | High | Low | Vbad |
| 8 | Low | Low | High | Medium | Bad |
| 9 | Low | Low | High | High | Bad |
| 10 | Low | Medium | Low | Low | Vbad |
| 11 | Low | Medium | Low | Medium | Bad |
| 12 | Low | Medium | Low | High | Bad |
| 13 | Low | Medium | Medium | Low | Bad |
| 14 | Low | Medium | Medium | Medium | Satisfactory |
| 15 Q | Low | Medium | Medium | High | Satisfactory |
| 16 | Low | Medium | High | Low | Bad |
| 17 | Low | Medium | High | Medium | Satisfactory |
| 18 | Low | Medium | High | High | Satisfactory |
| 19 | Low | High | Low | Low | Bad |
| 20 - | Low | High | Low | Medium | Bad |
| 21 | Low | High | Low | High | Bad |
| 22 | Low | High | Medium | Low | Bad |
| 23 | Low | High | Medium | Medium | Satisfactory |
| 24 | Low | High | Medium | High | Satisfactory |
| 25 | Low | High | High | Low | Bad |
| 26 | Low | High | High | Medium | Satisfactory |
| 27 | Low | High | High | High | Satisfactory |
| 28 | Medium | Low | Low | Low | Vbad |
| 29 | Medium | Low | Low | Medium | Bad |
| 30 | Medium | Low | Low | High | Bad |
| 31 | Medium | Low | Medium | Low | Bad |
| 32 | Medium | Low | Medium | Medium | Satisfactory |
| 33 | Medium | Low | Medium | High | Satisfactory |
| 34 | Medium | Low | High | Low | Bad |
| 35 | Medium | Low | High | Medium | Satisfactory |
| 36 | Medium | Low | High | High | Satisfactory |
| 37 | Medium | Medium | Low | Low | Bad |
| 38 | Medium | Medium | Low | Medium | Satisfactory |
| 39 | Medium | Medium | Low | High | Satisfactory |
| 40 | Medium | Medium | Medium | Low | Satisfactory |
| 41 | Medium | Medium | Medium | Medium | Good |
| 42 | Medium | Medium | Medium | High | Good |
| 43 | Medium | Medium | High | Low | Satisfactory |
| 44 | Medium | Medium | High | Medium | Good |
| 45 | Medium | Medium | High | High | Good |
| 46 | Medium | High | Low | Low | Bad |
| 47 | Medium | High | Low | Medium | Satisfactory |
| 48 | Medium | High | Low | High | Satisfactory |
| 49 | Medium | High | Medium | Low | Satisfactory |
| 50 | Medium | High | Medium | Medium | Good |


| Table B.2 (continued) |  |  |  |  | High |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 51 | Medium | Medium | High | Good |  |
| 52 | Medium | High | High | Low | Satisfactory |
| 53 | Medium | High | High | Medium | Good |
| 54 | Medium | High | High | High | Vgood |
| 55 | High | Low | Low | Low | Vbad |
| 56 | High | Low | Low | Medium | Bad |
| 57 | High | Low | Low | High | Bad |
| 58 | High | Low | Medium | Low | Bad |
| 59 | High | Low | Medium | Medium | Satisfactory |
| 60 | High | Low | Medium | High | Satisfactory |
| 61 | High | Low | High | Low | Bad |
| 62 | High | Low | High | Medium | Satisfactory |
| 63 | High | Low | High | High | Satisfactory |
| 64 | High | Medium | Low | Low | Bad |
| 65 | High | Medium | Low | Medium | Satisfactory |
| 66 | High | Medium | Low | High | Satisfactory |
| 67 | High | Medium | Medium | Low | Satisfactory |
| 68 | High | Medium | Medium | Medium | Good |
| 69 | High | Medium | High | Good |  |
| 70 | High | Medium | High | Low | Satisfactory |
| 71 | High | High | Medium | Good |  |
| 72 | High | Medium | High | High | Good |
| 73 | High | High | Low | Low | Bad |
| 74 | High | High | Low | Medium | Satisfactory |
| 75 | High | High | Low | High | Satisfactory |
| 76 | High | High | Medium | Low | Satisfactory |
| 77 | High | High | Medium | Medium | Good |
| 78 | High | High | Medium | High | Vgood |
| 79 | High | High | High | Low | Satisfactory |
| 80 | High | High | High | Medium | Vgood |
| 81 | High | High | High | High | Vgood |

Table B.3. Rule application for Economic sustainability assessment (27 Rules)

| No. | IF $($ CY $)=$ | AND $($ Ystab $)=$ | AND (GR) $=$ | ECONsus $=$ |
| :--- | :--- | :--- | :--- | :--- |
| 1 | Low | Low | Low | Vbad |
| 2 | Low | Low | Medium | Bad |
| 3 | Low | Low | High | Bad |
| 4 | Low | Medium | Low | Bad |
| 5 | Low | Medium | Medium | Satisfactory |
| 6 | Low | Medium | High | Satisfactory |
| 7 | Low | High | Low | Bad |
| 8 | Low | High | Medium | Satisfactory |
| 9 | Low | High | High | Good |
| 10 | Medium | Low | Low | Bad |
| 11 | Medium | Low | Medium | Satisfactory |
| 12 | Medium | Low | High | Satisfactory |
| 13 | Medium | Medium | Low | Satisfactory |
| 14 | Medium | Medium | Medium | Satisfactory |
| 15 | Medium | High | High | Good |
| 16 | Medium | High | Low | Satisfactory |
| 17 | Medium | High | Medium | Good |
| 18 | Medium | Low | High | Good |
| 19 | High | Low | Low | Bad |
| 20 | High | Low | High | Satisfactory |
| 21 | High | Medium | Low | Satisfactory |
| 22 | High | Medium | Medium | Satisfactory |
| 23 | High | Medium | High | Good |
| 24 | High | High | Low | Good |
| 25 | High | High | Medium | Satisfactory |
| 26 | High | High | High | Good |
| 27 | High |  |  | Vgood |
|  |  |  |  |  |

Table B.4. Rule application for Social sustainability assessment (9 Rules)

| No. | IF $($ ISS $)=$ | AND $($ FFS $)=$ | ECONsus $=$ |
| :--- | :--- | :--- | :--- |
| 1 | Low | Low | Vbad |
| 2 | Low | Medium | Bad |
| 3 | Low | High | Satisfactory |
| 4 | Medium | Low | Bad |
| 5 | Medium | Medium | Satisfactory |
| 6 | Medium | High | Good |
| 7 | High | Low | Satisfactory |
| 8 | High | Medium | Good |
| 9 | High | High | Vgood |

## Appendix C

## Maps of Myanmar



Figure C.1. Administrative map of Myanmar
(Source: Ramakrishna, 2000)


Figure C.2. Rainfall isohyets in Myanmar
(Source: University of Yangon, Myanmar)


Figure C.3. Isotherms in Myanmar

## (Source: University of Yangon, Myanmar)



Figure C.4. Soils in Myanmar
(Source: FAO, Rome, Italy)

## Appendix D

## Software Used

For this research, a powerful analysis software (MATLAB 7.1, Release 14 SP3 student version from Mathworks Inc., Fuzzy logic toolbox) is used for SAFE (Sustainability Analysis by Fuzzy Evaluation) methodology.

SPSS version 13 software is used for analyzing each indicator by using descriptive statistics and compare means.

Then, for Multi-criteria Evaluation, Microsoft Office Excel 2003 software is used to visualize the Amoeba or Radar diagram. SIA (Sustainability Indicator Analysis) and all the basic calculation are calculated by Microsoft Office Excel 2003 to get the comparable values.

The required softwares are supported by MCC (multiple Cropping Center, Chiang Mai University) for this study.

## Curriculum Vitae



